

dimer C of 1,3-dimethylthymine (Camerman, Weinblum & Nyburg, 1969).

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The Structure of the Orthorhombic Amphibole Holmquistite

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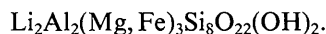
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A two-dimensional refinement of the structure of holmquistite has shown segregation of the cations in different sites. Iron is preferentially concentrated in the sites *M1* and *M3* which are internal to the chains, and lithium in the essentially inter-chain site *M4*. It is concluded that aluminum is concentrated in the site *M2* which has both intra- and inter-chain coordinations.

1. Introduction

Holmquistite is a lithium aluminum amphibole whose ideal formula can be written as



It was shown by Vogt, Bastiansen & Skancke (1958) to be a member of the orthorhombic series of amphiboles, and it was suggested by Whittaker (1960) that this was associated with the small size of the lithium ion. More recently, Ginsburg (1965) has also found a monoclinic holmquistite.

The structure of orthorhombic holmquistite is of interest for two reasons:

(i) Very little detailed information is available on the structure of any orthorhombic amphibole. The structure

of anthophyllite was determined in principle by Warren & Modell (1930), and further work was done on the same mineral by Ito (1950), but no refinement of its structure has been published. No structural study of any other orthorhombic amphibole has been reported.

(ii) In the monoclinic alkali amphiboles in which the alkali ion is sodium, this ion is confined to a single crystallographic site by its size. In magnesio-riebeckite (Whittaker, 1949) and glaucophane II (Ernst, 1963; Colville, Ernst & Gilbert, 1966; Papike & Clark, 1968) the trivalent ion [Fe^{III} and Al respectively] is also ordered to a considerable extent, and its ordering may be regarded as consequential on the effect of the confinement of the monovalent ion to a single neighbouring site. In holmquistite the primary effect of size will not lead to a marked ordering of the lithium into a particular site, and any ordering of the cations among the

four available sites will be of considerable interest, as arising from other causes.

2. Material

The specimen studied was from the Benson Pegmatite Mine, Mtoko, Rhodesia, which has been described and analysed by von Knorring & Hornung (1961). Its formula calculated to $24(\text{O}, \text{OH}, \text{F})$ is $\text{Na}_{0.03}\text{K}_{0.01}\text{Ca}_{0.03}\text{Li}_{1.79}\text{Mg}_{1.76}\text{Fe}_{1.21}^{2+}\text{Fe}_{0.24}^{3+}\text{Mn}_{0.03}\text{Ti}_{0.02}\text{Al}_{1.84}^{61}\text{Si}_{7.89}\text{Al}_{0.11}^{41}\text{O}_{22}(\text{OH})_{1.86}\text{F}_{0.08}\text{O}_{0.06}^{2-}$. Apparently single crystals are easily isolated from the rather friable material, but they tend to contain low-angle boundaries and give multiple spots on high layer lines. It proved difficult to choose sufficiently perfect crystals by the criterion of uniformity of extinction in the polarizing microscope, but the ninth crystal selected gave tolerably suitable reflexions. It measured approximately $0.3 \times 0.1 \times 0.015$ mm, the major dimension being parallel to c and the minor dimension parallel to a .

3. Unit cell and space group

Approximate unit-cell dimensions, obtained from oscillation and zero-layer Weissenberg photographs about the c axis, were: $a=18.29$, $b=17.67$, $c=5.28$ Å. Systematic absences agree with the space group $Pnma$ assigned to anthophyllite by Warren & Modell (1930). There is an additional non-space-group absence in that $hk0$ is present only for $h+2k=4n$ (including $h00$ only for $h=4n$). Warren & Modell reported 200 and 600 as weak and 10,0,0 and 14,0,0 as absent, although it is difficult to reconcile the presence of 200 and 600 with the structure proposed by these authors. $h00$ reflexions with $h \neq 4n$ could occur only if the two silicate double chains in each talc-like strip of the amphibole structure were at different distances from the metal cations sandwiched between them. Any such departure from equality would be expected to be very small, and would therefore lead to weak high-order reflexions of this type, and absent low-order ones, rather than *vice versa*. In the present work the complete absence of $hk0$ for $h+2k \neq 4n$, up to at least 34 orders of h and k shows that in holmquistite this non-space-group symmetry is very precise. As a result, the projection down the c axis has the two-dimensional space-group cm with an a axis which is half of that of the three-dimensional cell. This two-dimensional space-group is identical with that of the c axis projection of the monoclinic amphiboles.

4. Two-dimensional refinement

The intensities of the $hk0$ reflexions were measured from a range of multiple film exposures on a Weissenberg goniometer using $\text{Cu } K\alpha$ radiation, and again using $\text{Mo } K\alpha$ radiation. The absorption coefficients for these radiations were 187 and 24.8 respectively. Absorption corrections were made on the KDF9 computer by means of a program based on the method of Busing & Levy (1957) and modified by T. Blundell. In spite of the small size of the crystal, the absorption corrections for $\text{Cu } K\alpha$ radiation were large, and, in view of uncertainties in the crystal dimensions and in the adequacy of the program for such large corrections, the corrected $\text{Cu } K\alpha$ data were not considered very reliable. It was for this reason that the data were collected again with $\text{Mo } K\alpha$ radiation. However, as a check on the reliability of the results, the structure was refined independently from these two independent sets of data by means of a least-squares program based on that of Mills & Rollett (1961).

In view of the considerations in section 3, refinement was carried out in the two-dimensional space-group cm starting from estimated atomic positions based on clino-amphibole structures. In the following discussion the nomenclature of the sites follows that which is customary for clino-amphiboles (see, for example, Fig. 2 of Whittaker, 1960), not that introduced by Warren & Modell (1930) for anthophyllite.

The main interest of the two-dimensional refinement lies in the occupation of the cation sites $M3$, $M1$, $M2$ and $M4$ (listed in sequential order from the centres to outer edges of the cation bands). It was obviously desirable to start from the assumption of completely random occupation of the four sites by all the available cations. Since it is not practicable to refine more than one occupation parameter per site, such a situation was simulated by assuming all sites to be occupied by $0.6 \text{ Li} + 0.4 \text{ Fe}$, which gives an atomic scattering factor approximating to random occupancy by all the cations in the formula. Refinement of a single occupation parameter for each of the four sites (together with an overall temperature factor and the variable positional parameters permitted by the two-dimensional space-group) could then be expected to indicate any preferential occupation of a site in terms of relative average scattering factors. The results from the first cycles of refinement showed the scattering factor at $M4$ to be so small that this site must be almost entirely occupied by Li. The scattering factors at $M1$ and $M3$ were so large that

Table 1. Occupation of cation sites from least-squares refinement

	Cu data	Mo data	σ_{Cu}	σ_{Mo}	Interpretation to accord with formula
$M1$	$\text{Mg}_{0.61}\text{Fe}_{0.39}$	$\text{Mg}_{0.56}\text{Fe}_{0.44}$	0.06	0.04	$\text{Mg}_{0.52}\text{Fe}_{0.48}$
$M2$	$\text{Al}_{1.14}\text{Fe}_{0.14}$	$\text{Al}_{1.01}\text{Fe}_{0.01}$	0.06	0.04	$\text{Al}_{0.92}\text{Mg}_{0.08}$
$M3$	$\text{Mg}_{0.68}\text{Fe}_{0.32}$	$\text{Mg}_{0.49}\text{Fe}_{0.51}$	0.08	0.05	$\text{Mg}_{0.46}\text{Fe}_{0.54}$
$M4$	$\text{Li}_{0.80}\text{Mg}_{0.15}$	$\text{Li}_{0.94}\text{Mg}_{0.01}$	0.08	0.06	$\text{Li}_{0.90}\text{Mg}_{0.05}\text{Na}_{0.03}$
A	$\text{Ca}_{0.08}$	$\text{Ca}_{0.03}$	0.06	0.02	$(\text{Ca}, \text{K})_{0.04}$

these sites must contain most of the iron, while the occupancy of *M2* was compatible with Mg or Al (the alternative of a mixture of Li and Fe at *M2* being ruled out by the limited amount of Li available for attribution to *M4*). Further refinement was then carried out with Mg+Fe at *M1* and *M3*, Al+Fe at *M2* and Li+Mg at *M4*. The initial ratios of these ions in these sites were chosen to be in line both with the formula and with the results of the first refinement based on Li+Fe only.

Because it seems improbable that the large cations K, Na, and Ca could be accommodated in the *M4* site of an orthorhombic amphibole, an open-ended parameter was introduced in one cycle of the refinement to permit the placing of these ions at the vacant *A* site. Refinement did not lead to a significant non-zero occupancy for this site.

The process of refinement described above led to *R* values of 0.198 and 0.165 for the Cu *Kα* and Mo*Kα* data respectively. Further refinement of positional and independent isotropic temperature factors (holding occupancies constant) led to a further reduction of *R* to 0.085 for the Mo *Kα* data. This further refinement was not carried out for the Cu *Kα* data.

The final occupancies derived from the two sets of data are shown in Table 1, and are mutually confirmatory, at least in general outline.

The positional parameters derived from the Cu *Kα* data were quite evidently less satisfactory than those from the Mo *Kα* data. For example, the projected Si1–O1 and Si2–O2 distances were noticeably unequal. These irregularities were not confirmed by the Mo *Kα* data, and accordingly the atomic positions given in Table 2 are those derived from the Mo *Kα* data only.

Table 2. Atomic positions and isotropic temperature factors

	<i>x/a</i>	<i>y/b</i>	<i>B</i>
O1	0.110	0.095	0.31
O2	0.119	0.175	0.37
O3	0.115	0	0.88
O4	0.122	0.249	0.36
O5	0.143	0.364	0.49
O6	0.156	0.382	0.32
O7	0.165	0.500	0.41
Si1	0.289	0.087	0.13
Si2	0.299	0.173	0.30
M1	0	0.091	0.37
M2	0	0.182	0.02
M3	0	0	0.16
M4	0	0.262	1.07

5. Discussion

The results of the refinements of the occupancies of the cation sites, given in columns 2 and 3 of Table 1, take no specific account of the numbers of atoms available as given by the formula. They were refined subject only to the condition that in *M1*, *M2* and *M3*, the

Table 3. Observed and calculated structure factors for planes *hk0*

<i>x</i>	<i>F_o</i>	<i>F_c</i>	<i>k</i>	<i>F_o</i>	<i>F_c</i>	<i>h</i>	<i>F_o</i>	<i>F_c</i>	<i>k</i>	<i>F_o</i>	<i>F_c</i>	<i>h</i>	<i>F_o</i>	<i>F_c</i>
h = 0														
4	7332	-7060	1	10122	10354	0	6836	6715	1	2761	2767	5	1230	1230
6	868	429	3	2010	-4639	2	719	556	5	1523	1386	9	1771	-1362
8	2525	1985	5	3538	-9759	4	1153	-1310	7	1767	1865	11	1758	2800
10	6316	6829	7	5254	1625	6	2127	3164	9	2980				
12	10565	11588	9	7090	10121	8	3520	1071	11	5101	2074			
14	14169	-4079	11	8955	6120	10	4997	2365	13	637	713			
16	18354	11522	13	11577	1121	12	1608	1901	15	2023	2150			
18	23098	-758	15	1399	-304	14	1864	1965	17	3166	3684			
20	29469	-879	17	1653	797	16	2595	523	19	4609	1012			
22	37494	3909	19	1921	-1731	18	3539	1955	21	6302	6332			
24	47298	-3767	21	2282	6236	20	4825	1659	23	8366	-946			
26	59984	1509	23	2758	1073	22	6568	1914	25	11069	1012			
28	75772	-3304	25	3382	1914	24	9079	2426	27	14544	-3454			
h = 2														
3	967	863	0	2382	-1883	3	3067	-2338	10	5496	3167			
5	2617	2103	6	5228	2358	1	919	880	12	5991	6169	3	1123	1209
7	4786	-2414	8	760	-620	7	3620	-3324	16	2519	-2272	9	1209	1323
9	725	65	10	2559	-2498	11	5191	-3133	22	3551	-1616			
11	1039	6696	12	3598	3619	13	6837	8805	16	1259	-1416			
13	1325	408	14	4640	-2353	14	8772	-3641	26	1711	1022	0	1660	1208
15	1601	-1131	20	566	-679	17	1082	-360						
17	1878	1509	22	2866	2666	19	1425	-1392	5	227	-282	2	863	1507
19	2154	1201	24	4050	669	21	1732	1622	3	527	-1639	6	921	1129
21	2429	1509	26	5470	-1200	23	2265	-651	9	1396	1228			
23	2704	1809	28	7146	1530	25	3027	-988	11	2251	2153	1	3039	3026
h = 4														
0	2010	-1224	3	3752	3635	23	2162	2121	23	1830	1614	11	3127	3185
2	698	532	5	1481	616	0	2571	4373	0	1924	-1714			
4	4133	2536	7	2354	1039	6	3623	1956	6	2508	1378			
6	1566	1172	9	3021	1956	8	4923	985	8	3583	988	0	2012	2264
8	1634	1697	11	2606	-3537	6	1025	-945	2	1508	1508			
10	611	-768	13	1695	-1501	6	2121	1929	4	1193	1587			
12	770	501	15	3394	3208	10	1465	1427	8	1566	1508			
14	1659	1567	17	559	-79	16	1705	1269	12	2262	-2183			
16	2569	2569	19	826	-784	16	1688	1616	16	1270	1361			
18	1678	-1828	21	1207	1334	18	1199	-1219	12	1270	1361			
20	967	208	23	2292	-2193	20	1807	1919	18	1193	1133			
22	1533	1697	25	3128	1829	22	1608	1624	20	1117	1019			
			27	877	1185	24	1802	1912	20	1227	-1160			
			29	675	173	26	2169	2207						
			31	1299	-1568									

The range of planes listed is extended to include the rather large *F_o* values for *k* in the region of 30, although this means that a rather large number of reflexions within this range of indices were unobserved. 63 planes with *F_o*=0 occur within this range and are not listed. Two reflexions, 020 and 210, were at too small an angle to be measured with Mo radiation and are also omitted, although their approximate values are known from the Cu data.

The interpretation in the final column was obtained as follows. The distribution of Al between octahedral and tetrahedral sites, indicated in the formula given in section 2, was derived in the usual way by allocating sufficient Al to tetrahedral sites to make up 8 atoms of Si+Al^[4]. For reasons discussed in the next paragraph, the predominant cation at *M2* is assumed to be Al, although, of course, the diffraction results do not distinguish between Al and Mg. Therefore all the Al^[6] in the formula is put at *M2*. The total Fe content derived from column 3 (1.39 allowing for multiplicity of sites) is slightly less than the total Fe+Ti+Mn in the formula. The Fe (including Ti+Mn) in *M1* and *M3* has therefore been scaled up to fit the formula, and sufficient Mg put in these sites to fill them. The remaining Mg is put at *M2* and *M4*. All Li available is put at *M4* and the small amounts of Na, K and Ca, rather arbitrarily and without good evidence, are divided between *M4* and *A*.

The attribution of all the Al to the *M2* position in Table 1 is not strictly demanded by the data, which only indicates an avoidance of *M2* by Fe, and would be equally satisfied by occupation of that site by Mg. However, the effects of radius, charge and polarization would all be more likely to lead to an association

The attribution of all the Al to the *M2* position in Table 1 is not strictly demanded by the data, which only indicates an avoidance of *M2* by Fe, and would be equally satisfied by occupation of that site by Mg. However, the effects of radius, charge and polarization would all be more likely to lead to an association

between Mg and Fe than between Al and Fe, since the latter is predominantly Fe^{II} ; and the fact that there is evidence for occupation of $M2$ by the triply-charged ion in riebeckite and glaucophane, when $M4$ is occupied by a singly-charged ion, suggests that a similar situation may be expected here in view of the preferential occupation of $M4$ by Li. The apparent total avoidance of $M2$ by Fe is, however, difficult to understand in view of the presence of $\text{Fe}_{0.24}^{3+}$ in the formula. It has been shown by Bancroft, Maddock, Burns & Strens (1966) by means of infrared and Mössbauer spectra that in cummingtonite and anthophyllite Fe^{II} goes into $M4$ and $M2$ (in that order of preference) rather than into $M1$ and $M3$, on account of the greater crystal field stabilization energies arising in the former, less symmetrically coordinated, sites. The avoidance of $M4$ and $M2$ by Fe in holmquistite shows that the ordering observed here must be due to energy differences greater than those which would be involved in such crystal field effects. That the difference does not arise in any way from the presuppositions of the different experimental methods has been shown by infrared examination of holmquistite by Strens (1966). This revealed OH vibration frequencies appropriate to the occupation of $M1$ and $M3$ sites solely by Mg+Fe. Were Fe to be present in $M2$ or $M4$, the composition of the mineral would require a corresponding introduction of Al and Li into $M1$ and $M3$, and this would have led to additional OH vibration frequencies. Strens did not detect any difference in occupancy of the $M1$ and $M3$ sites, and this is in accordance with the fact that the occupancies deduced for these sites in Table 1 do not differ significantly from one another.

Since Li is undoubtedly small enough to fit the $M1$, $M2$ and $M3$ sites of amphibole, and since Mg and Fe are known to be able to enter the $M4$ site in orthorhombic amphiboles, it would seem that the preferential entry of Li into $M4$ must be an effect of electrostatic potential leading to a preference for a low positive charge at $M4$ combined with a high positive charge at $M2$. The preference for a low charge at $M4$ may perhaps be qualitatively correlated with the fact that two of the six oxygen atoms which coordinate this site are already attached to two silicon atoms each, and any electrostatic bonds formed from them to $M4$ necessarily contravene Pauling's second rule. A more quantitative theoretical investigation of electrostatic ordering effects on cations in amphibole structures is in hand.

The relative positions of the atoms in the projection are in accord with the now familiar details of clino-amphibole structures, with the silicate band bending about its mid-line away from the plane of the metal ions. Calculated standard deviations for atomic positions are 0.02 Å for oxygen, 0.01 Å for silicon, $M1$ and $M2$, and 0.06 Å for $M4$ (lithium). It is not worth while seeking to interpret the positions in detail before the completion of a three-dimensional refinement which is in hand. It is, however, worth noting that in spite of the large uncertainty in the y coordinate of $M4$ (arising from the low electron density associated with it), this is very significantly smaller than the corresponding coordinate in the calc-alkali clino-amphiboles in which this site is occupied by Na or Ca. It is, however, very similar to the coordinate of $M4$ found by Ghose (1961) and Fisher (1966) in cummingtonite.

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